

1. We will study some simple B-model boundary conditions for a target space  $X$ .
  - (a) Dirichlet boundary conditions fix the boundary value of the sigma-model scalar fields. They are labelled by a point  $p$  in  $X$ . In the formulation in terms of maps into  $T^*[1]X$  they are associated to the Lagrangian fiber above a point in  $T^*[1]X$ . Find the classical boundary local operators.
  - (b) Neumann boundary conditions leave the boundary value of the sigma-model scalar fields free to fluctuate. In the formulation in terms of maps into  $T^*[1]X$  they are associated to the zero section of  $T^*[1]X$ . Find the classical boundary local operators.
  - (c) Find the classical local operators at a junction point between Neumann and Dirichlet boundary conditions.
  - (d) What is the classical phase space of the theory on a segment, with Neumann boundary conditions? Compare the geometric quantization of that with the space of local operators at Neumann boundary conditions.
  - (e) How do your answers compare with calculations in the derived category of coherent sheaves?
2. A BBB brane on  $\mathbb{C}^2$  should be described by an instanton bundle, which in turns can be built from the ADHM data: two  $N \times N$  matrices  $B_i$ , an  $N \times K$  matrix  $I$  and an  $K \times N$  matrix  $J$ , which satisfy the constraints for an  $U(N)$  hyper-kahler quotient, where  $U(N)$  acts by conjugation on  $B_i$  and multiplication from the left/right on  $I$  and  $J$ .

- (a) The ADHM complex

$$\mathbb{C}^N \rightarrow \mathbb{C}^{2N+K} \rightarrow \mathbb{C}^N \tag{1}$$

uses differentials

$$\begin{pmatrix} J & B_2 + z_2 & -B_1 - z_1 \end{pmatrix} \tag{2}$$

$$\begin{pmatrix} I & B_1 + z_1 & B_2 + z_2 \end{pmatrix} \tag{3}$$

where  $z_i$  are coordinates on  $\mathbb{C}^2$ . Verify that the differential squares to 0.

- (b) The differential above can be interpreted as the supercharge in an  $N = 4$  SQM. Can you use the ADHM data to write three more supercharges for the SQM?